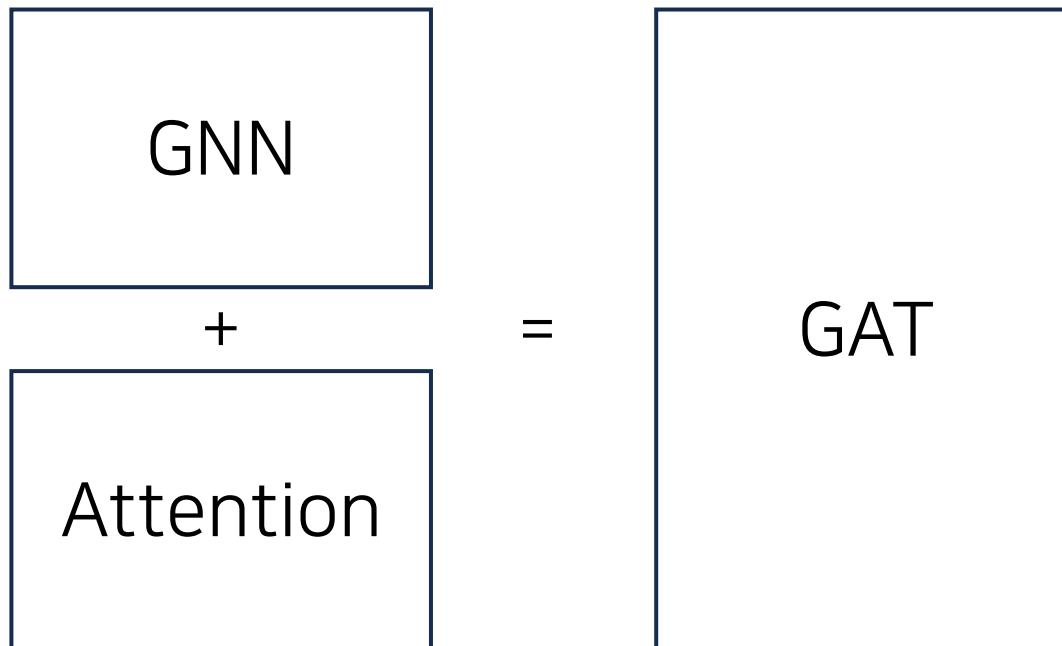


Graph Attention Networks

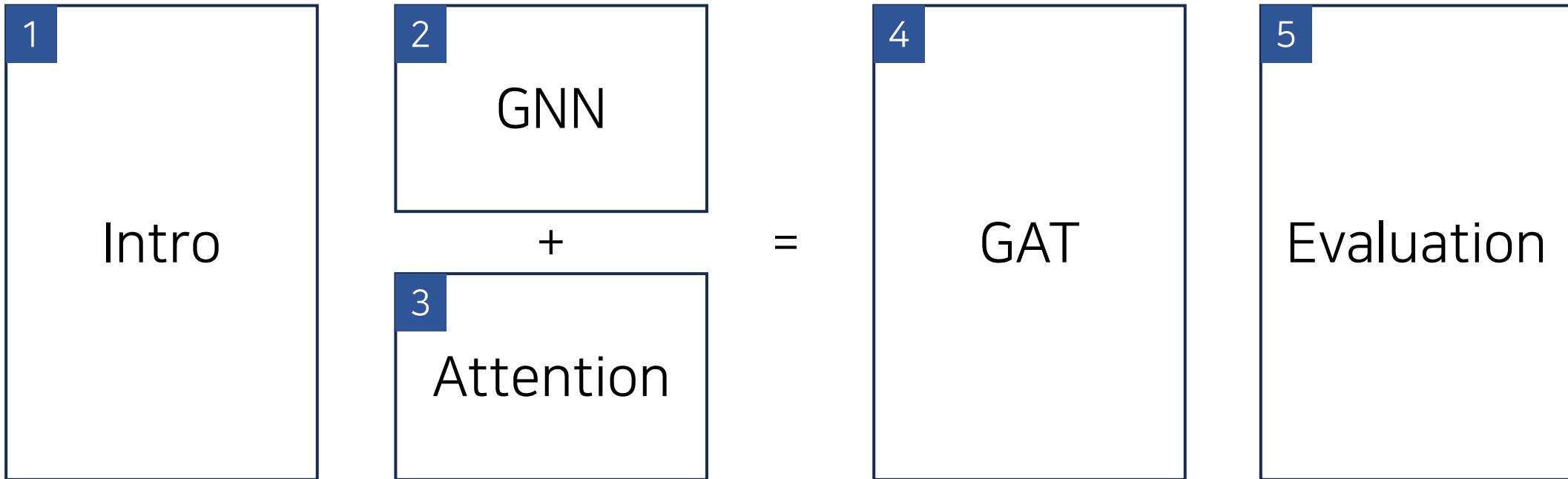
ICLR 2018

1. Intro



Graph Attention Networks

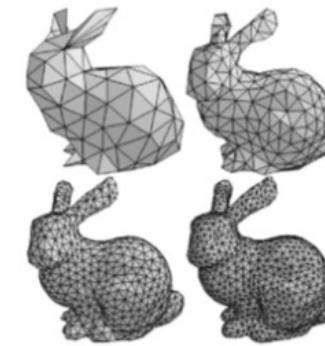
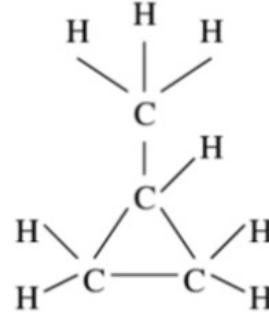
1. Intro



2. GNN

Graph Neural Network

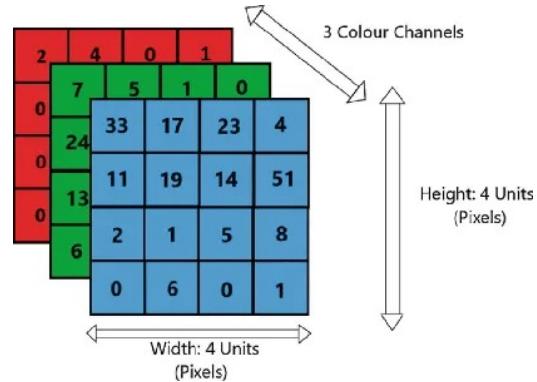
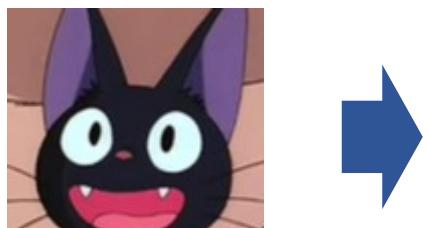
그래프 데이터에서의 Neural Network



2. GNN

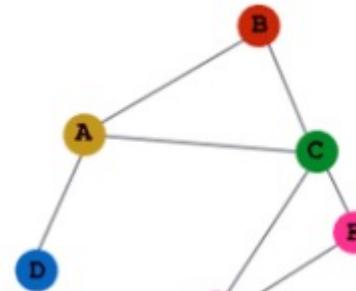
입력 데이터 표현 방법

Neural Network



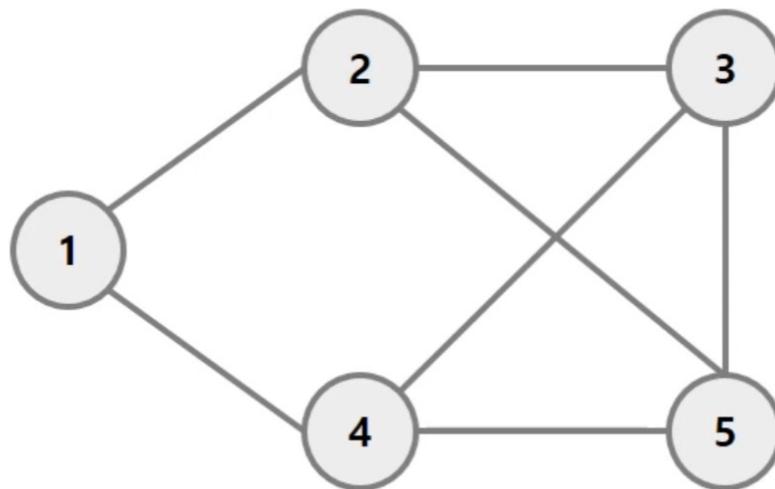
행렬의 형태로 표현

Graph Neural Network



2. GNN

입력 데이터 표현 방법 - Adjacency Matrix



[Adjacency Matrix]

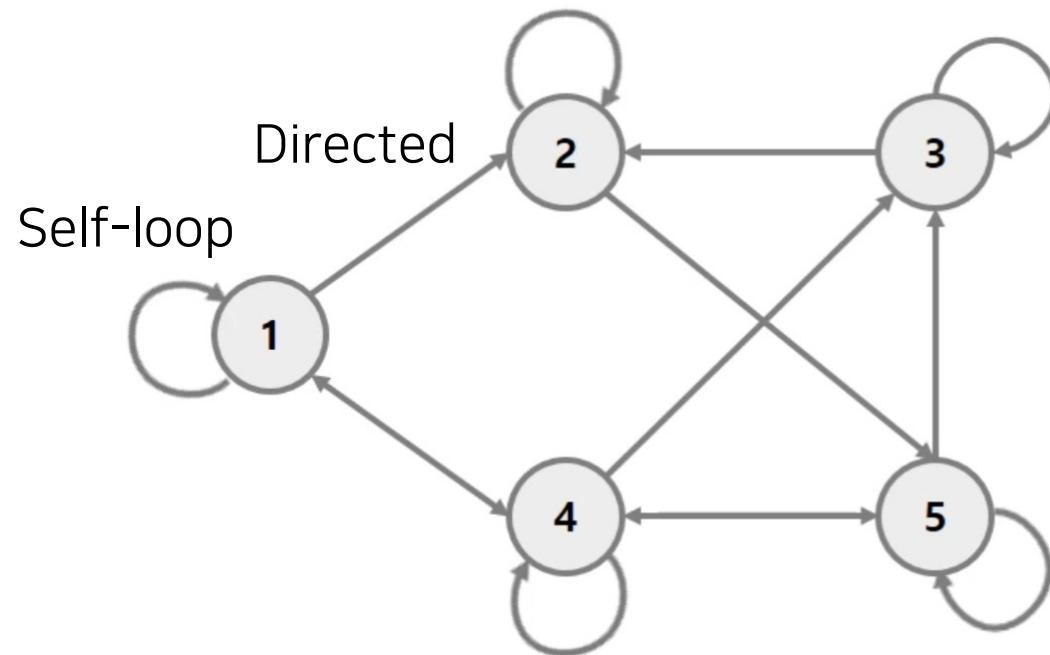
0	1	0	1	0
1	0	1	0	1
0	1	0	1	1
1	0	1	0	1
0	1	1	1	0

N

N

2. GNN

입력 데이터 표현 방법 - Adjacency Matrix



[Adjacency Matrix]

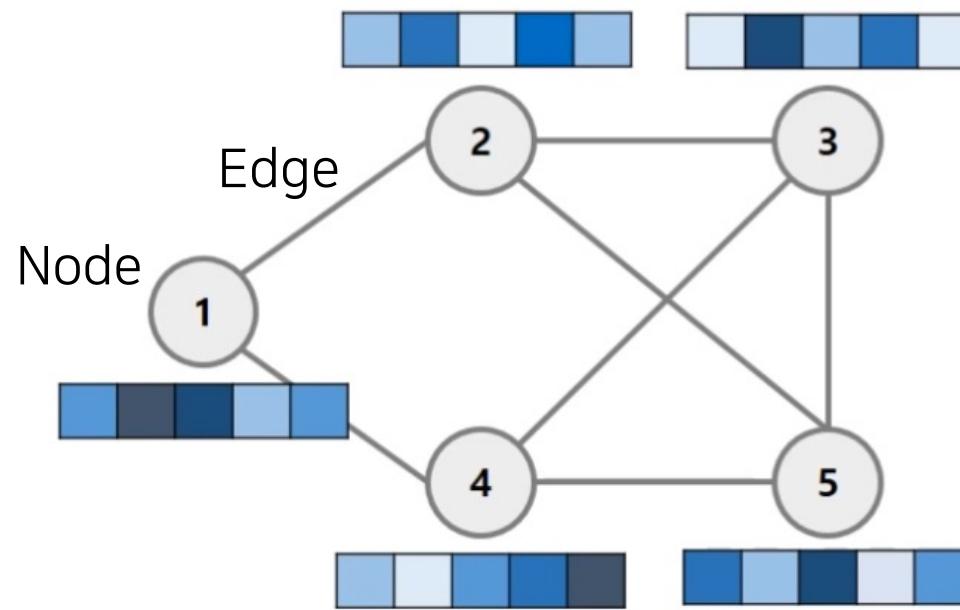
a_{11}	a_{12}	0	a_{14}	0
0	a_{22}	0	0	a_{25}
0	a_{32}	a_{33}	0	0
a_{41}	0	a_{43}	a_{44}	a_{45}
0	0	a_{53}	a_{54}	a_{55}

Weight

N

2. GNN

입력 데이터 표현 방법 - Node Feature



[Node-Feature Matrix]

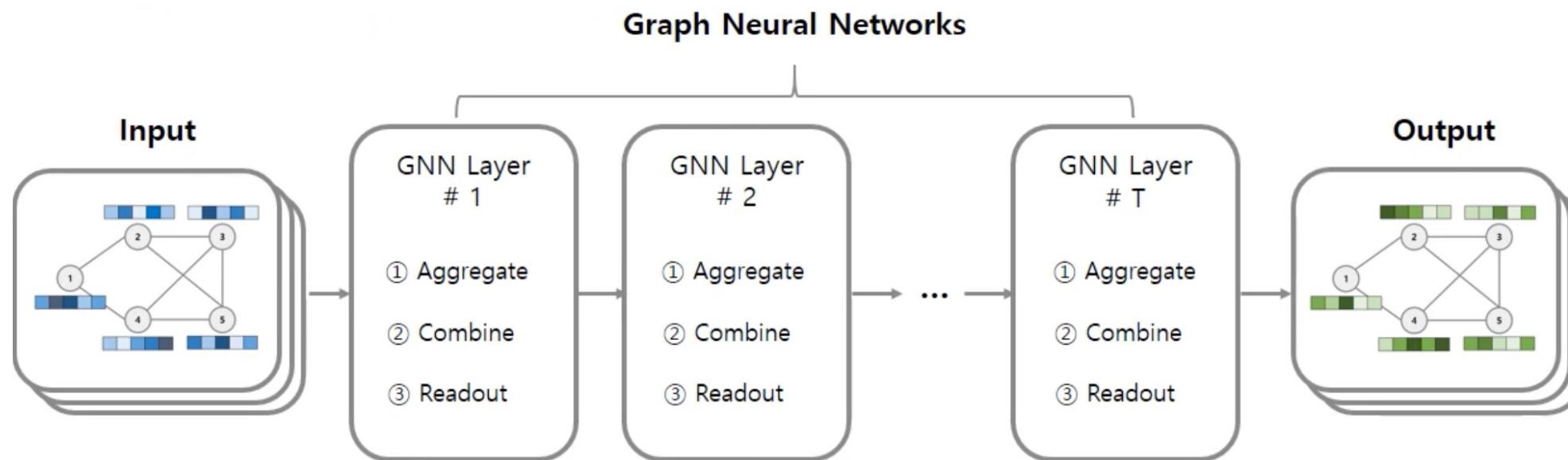
A 5x5 matrix representing the node-feature matrix. The columns are labeled D and the rows are labeled N. The matrix contains colored squares corresponding to the node features shown in the diagram. The matrix is as follows:

Light Blue	Dark Grey	Dark Blue	Light Blue	Light Blue
Light Blue	Dark Blue	Dark Blue	Light Blue	Light Blue
Light Blue	Dark Grey	Dark Blue	Light Blue	Light Blue
Light Blue	Dark Blue	Dark Blue	Light Blue	Light Blue
Light Blue	Dark Blue	Dark Blue	Light Blue	Dark Grey

2. GNN

Node Level Task 업데이트 과정

1. Aggregate / Message Passing
2. Combine / Update
3. Readout



3. Attention

Dictionary

Q: 오렌지

(일치하는지, 0,1)

Key (K)	Similarity Sim(K, Q)	Value (V)	Sim(K, Q) * V
레몬	0	새콤한맛	0
오렌지	1	달콤한맛	달콤한맛
아보카도	0	크레파스맛	0

-> 달콤한맛!

3. Attention

Dictionary -> Attention

Q: 꿀

(유사한 정도의 Softmax)

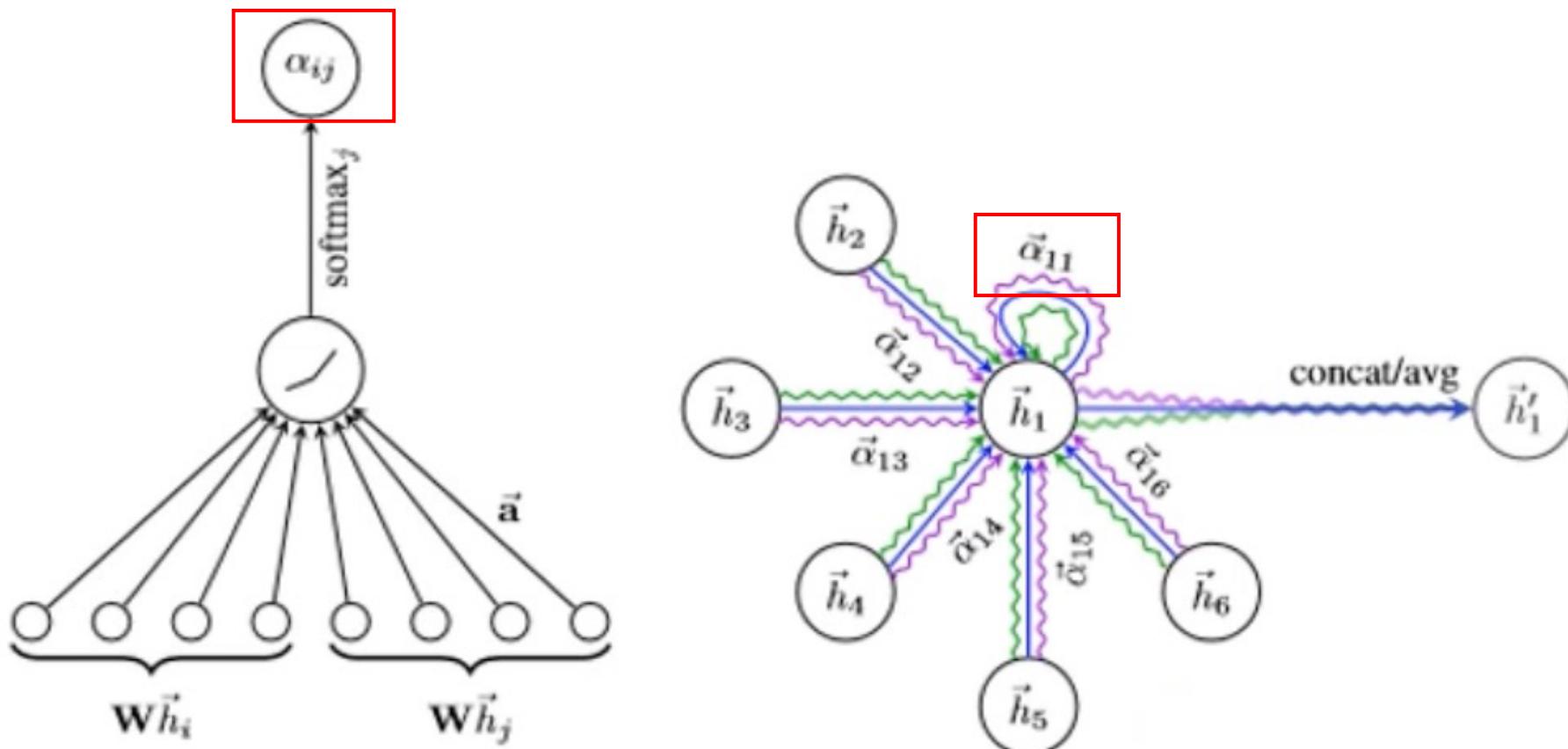
Key (K)	Similarity Sim(K, Q)	Value (V)	Sim(K, Q) * V
레몬	0.35	새콤한맛	0.35 * 새콤한맛
오렌지	0.64	달콤한맛	0.64 * 달콤한맛
아보카도	0.01	크레파스맛	0.01 * 크레파스맛

Attention Score

-> 새콤달콤한맛!

4. Graph Attention Network

Overview

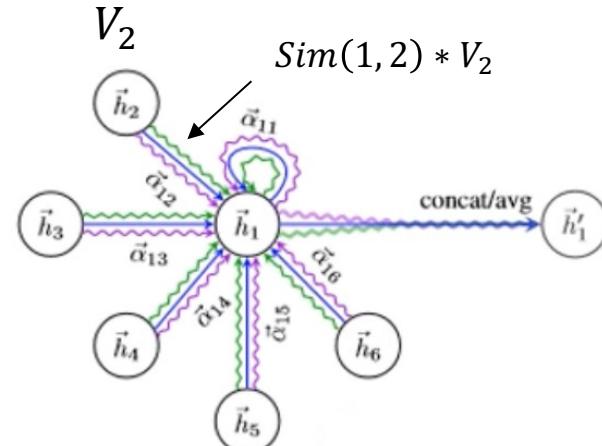
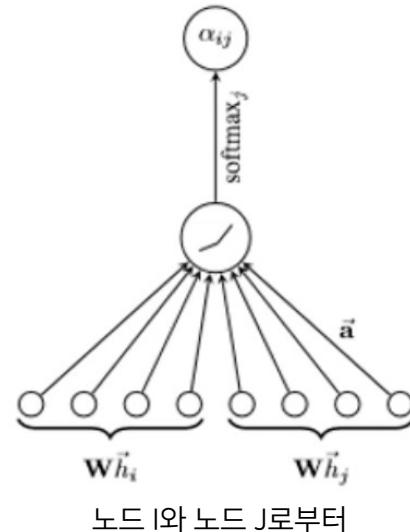


4. Graph Attention Network

Overview

모든 I, J쌍의 Sim 계산

$Sim(I, J)$



$Sim(I, J)$

V_2

$Sim(1, 2) * V_2$

Key (K)	Similarity $Sim(K, Q)$	Value (V)	$Sim(K, Q) * V$
레몬	0.35	새콤한맛	0.35 * 새콤한맛
오렌지	0.64	달콤한맛	0.64 * 달콤한맛
아보카도	0.01	크레파스맛	0.01 * 크레파스맛

4. Graph Attention Network

Aggregate

유사도 e_{ij} 계산

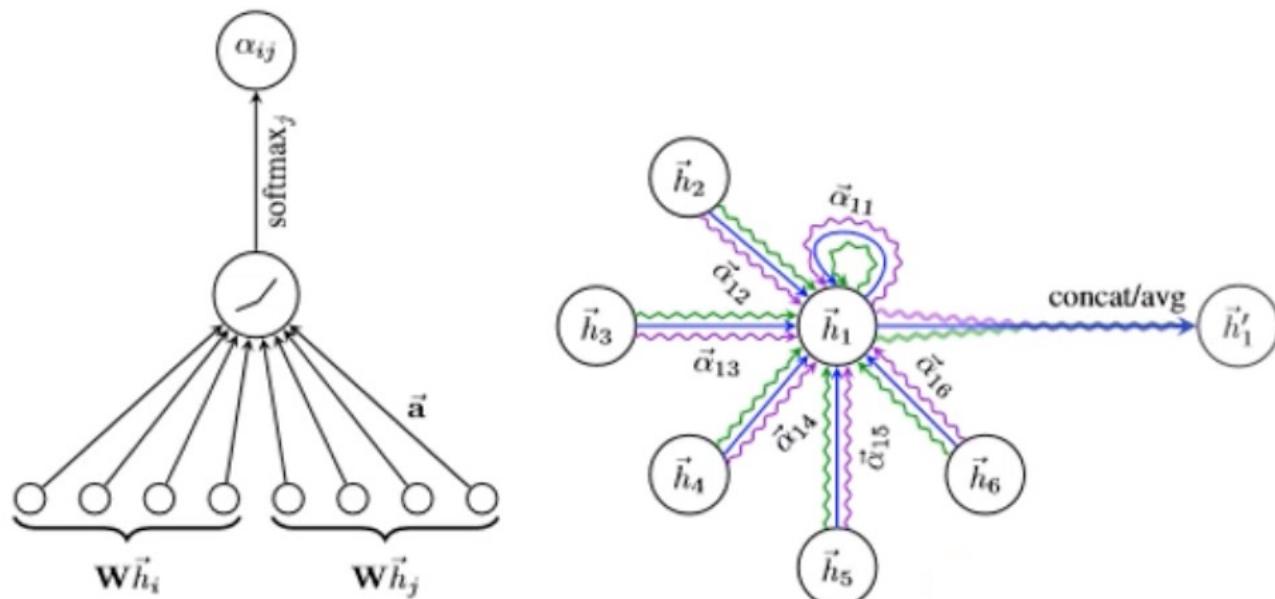
어텐션 스코어 a_{ij} 계산

Combine

이웃들의 정보 $a_{ij} \vec{W} \vec{h}_j$ 합계

Multi-head attention

Readout



4. Graph Attention Network

Aggregate

유사도 e_{ij} 계산

어텐션 스코어 a_{ij} 계산

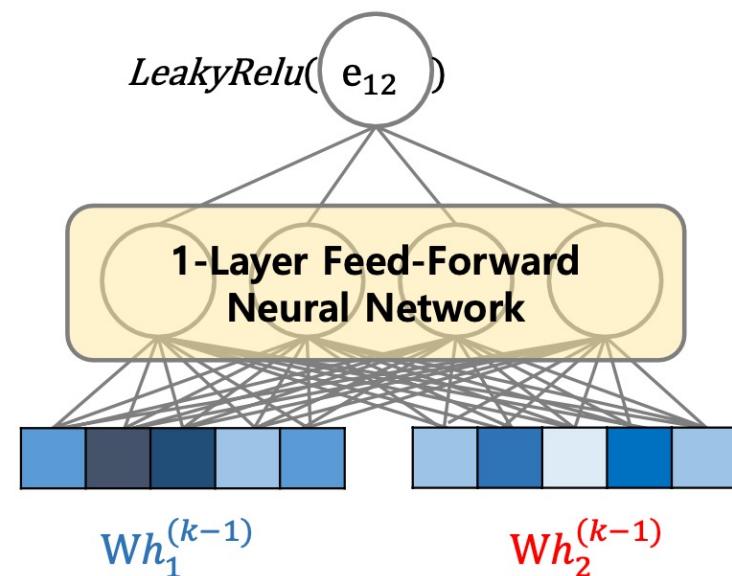
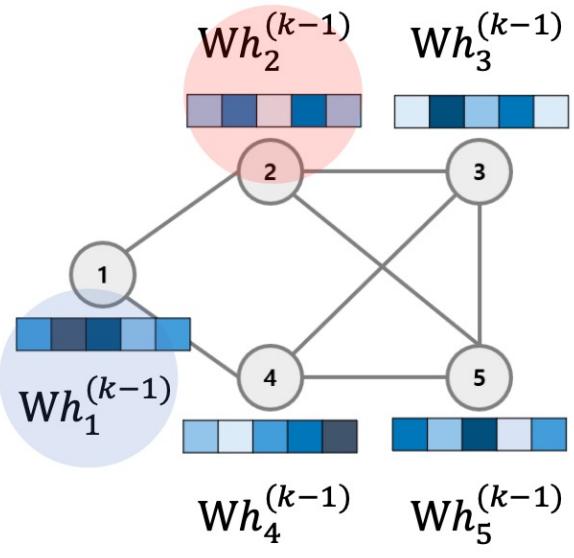
Combine

이웃들의 정보 $a_{ij} Wh_j$ 합계

Multi-head attention

Readout

아까의 $Sim(I, J)$ 와 유사



4. Graph Attention Network

Aggregate

유사도 e_{ij} 계산

어텐션 스코어 a_{ij} 계산

Combine

이웃들의 정보 $a_{ij} Wh_j$ 집계

Multi-head attention

Readout

아까의 $Sim(I, J)$ 와 유사

모든 노드들간의 유사도 계산

e_{11}	e_{12}	e_{13}	e_{14}	e_{15}
e_{21}	e_{22}	e_{23}	e_{24}	e_{25}
e_{31}	e_{32}	e_{33}	e_{34}	e_{35}
e_{41}	e_{42}	e_{43}	e_{44}	e_{45}
e_{51}	e_{52}	e_{53}	e_{54}	e_{55}

병렬적으로 계산 가능

3. Attention

Dictionary -> Attention

Q: 풀

(유사한 정도의 Softmax)

Key (K)	Similarity Sim(K, Q)	Value (V)	Sim(K, Q) * V
레몬	0.35	새콤한맛	0.35 * 새콤한맛
오렌지	0.64	달콤한맛	0.64 * 달콤한맛
아보카도	0.01	크레파스맛	0.01 * 크레파스맛

Attention Score

-> 새콤달콤한맛!

4. Graph Attention Network

Aggregate

유사도 e_{ij} 계산

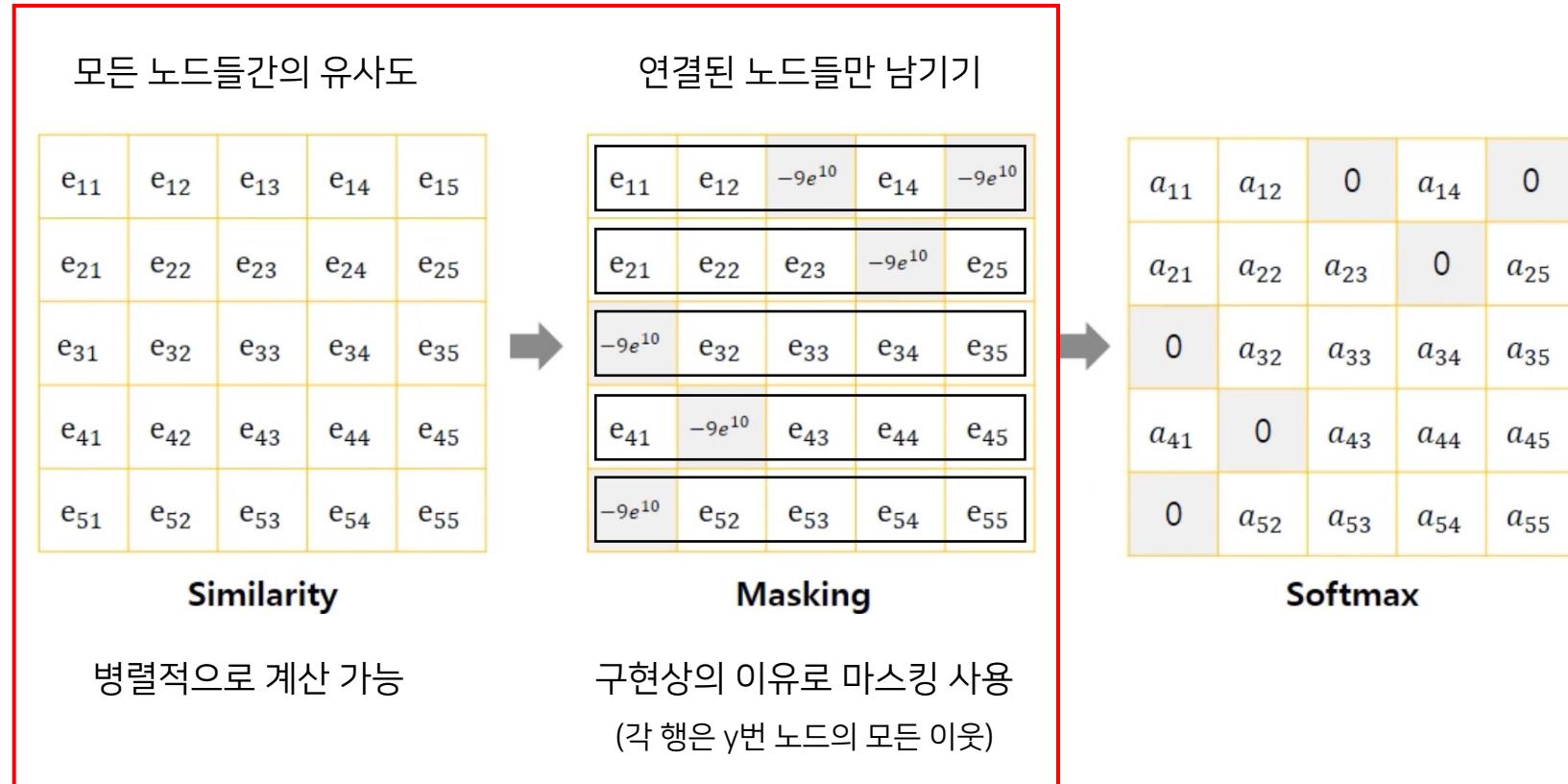
어텐션 스코어 a_{ij} 계산

Combine

이웃들의 정보 $a_{ij} Wh_j$ 합계

Multi-head attention

Readout



4. Graph Attention Network

Aggregate

유사도 e_{ij} 계산

어텐션 스코어 a_{ij} 계산

Combine

이웃들의 정보 $a_{ij} Wh_j$ 합계

Multi-head attention

Readout

모든 노드들간의 유사도

e_{11}	e_{12}	e_{13}	e_{14}	e_{15}
e_{21}	e_{22}	e_{23}	e_{24}	e_{25}
e_{31}	e_{32}	e_{33}	e_{34}	e_{35}
e_{41}	e_{42}	e_{43}	e_{44}	e_{45}
e_{51}	e_{52}	e_{53}	e_{54}	e_{55}

Similarity

병렬적으로 계산 가능

연결된 노드들만 남기기

e_{11}	e_{12}	e_{13}	e_{14}	$-9e^{10}$
e_{21}	e_{22}	e_{23}	e_{24}	$-9e^{10}$
$-9e^{10}$	e_{32}	e_{33}	e_{34}	e_{35}
e_{41}	$-9e^{10}$	e_{43}	e_{44}	e_{45}
$-9e^{10}$	e_{52}	e_{53}	e_{54}	e_{55}

Masking

구현상의 이유로 마스킹 사용
(각 행은 y 번 노드의 모든 이웃)

Softmax

a_{11}	a_{12}	0	a_{14}	0
a_{21}	a_{22}	a_{23}	0	a_{25}
0	a_{32}	a_{33}	a_{34}	a_{35}
a_{41}	0	a_{43}	a_{44}	a_{45}
0	a_{52}	a_{53}	a_{54}	a_{55}

Softmax

각 행마다, y 번 노드 기준
모든 이웃들과의 Attention score

4. Graph Attention Network

Aggregate

유사도 e_{ij} 계산

어텐션 스코어 a_{ij} 계산

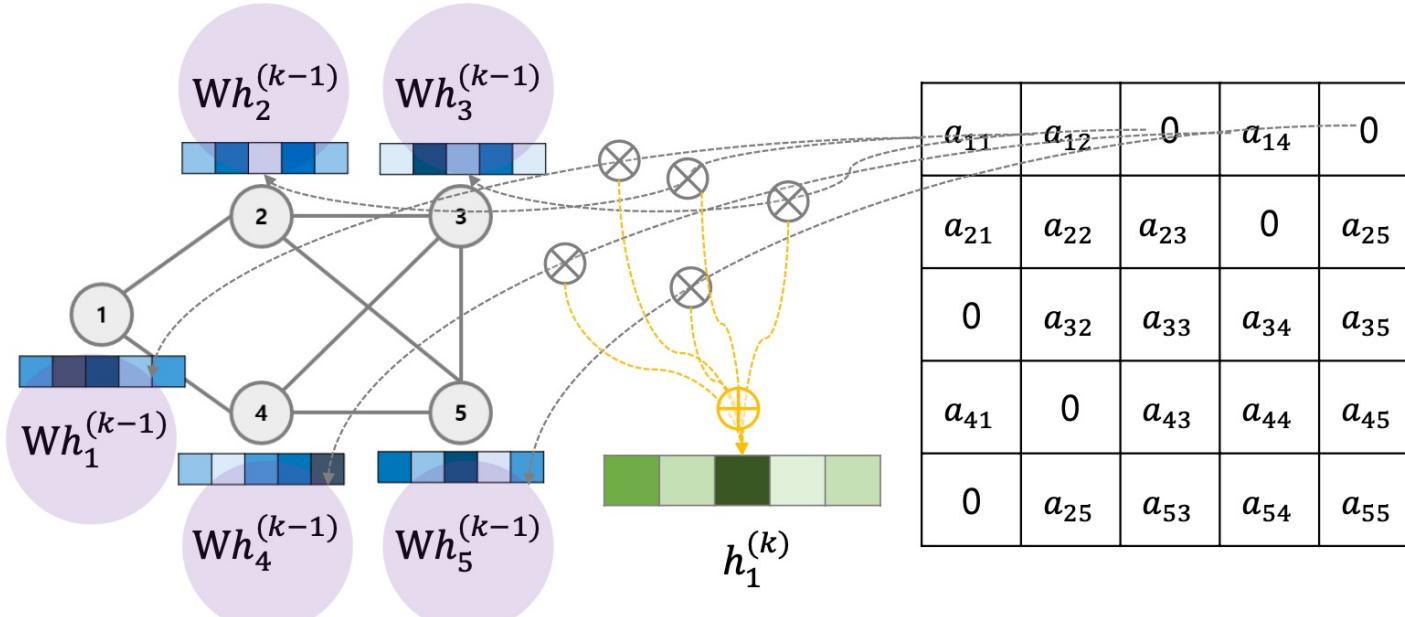
Combine

이웃들의 정보 $a_{ij} \mathbf{W} \mathbf{h}_j$ 집계

Multi-head attention

Readout

Key (K)	Score(K, Q)	Value (V)	Score(K, Q) * V
레몬	0.35	새콤한맛	0.35 * 새콤한맛
오렌지	0.64	달콤한맛	0.64 * 달콤한맛
아보카도	0.01	크레파스맛	0.01 * 크레파스맛



4. Graph Attention Network

Aggregate

유사도 e_{ij} 계산

어텐션 스코어 a_{ij} 계산

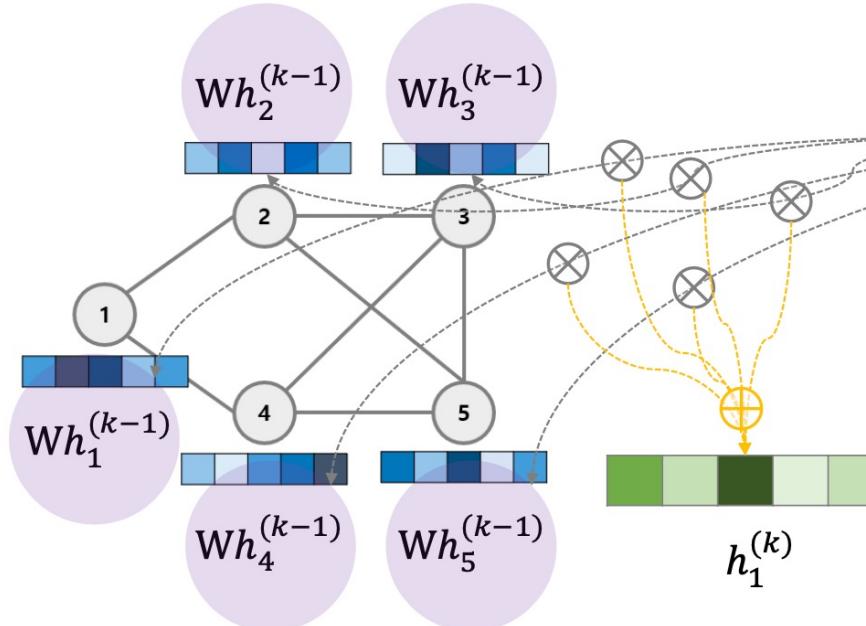
Combine

이웃들의 정보 $a_{ij} Wh_j$ 집계

Multi-head attention

Readout

Key (K)	Score(K, Q)	Value (V)	Score(K, Q) * V
레몬	0.35	새콤한맛	0.35 * 새콤한맛
오렌지	0.64	달콤한맛	0.64 * 달콤한맛
아보카도	0.01	크레파스맛	0.01 * 크레파스맛



a_{11}	a_{12}	0	a_{14}	0
a_{21}	a_{22}	a_{23}	0	a_{25}
0	a_{32}	a_{33}	a_{34}	a_{35}
a_{41}	0	a_{43}	a_{44}	a_{45}
0	a_{25}	a_{53}	a_{54}	a_{55}

모든 노드에 Self-loop 존재

4. Graph Attention Network

Aggregate

유사도 e_{ij} 계산

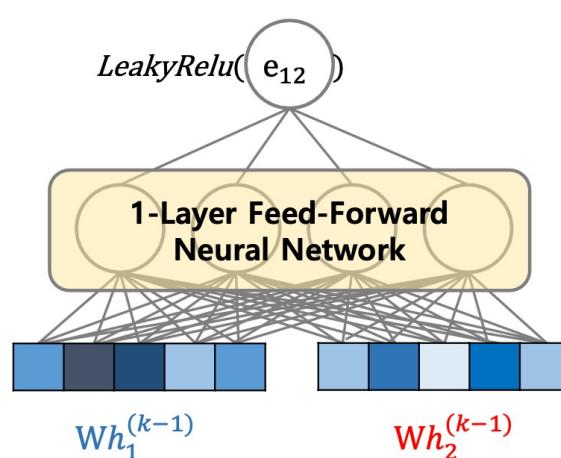
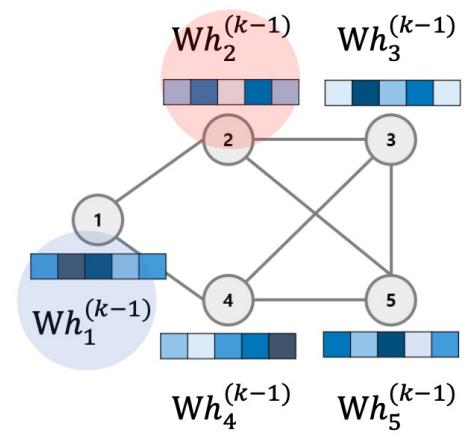
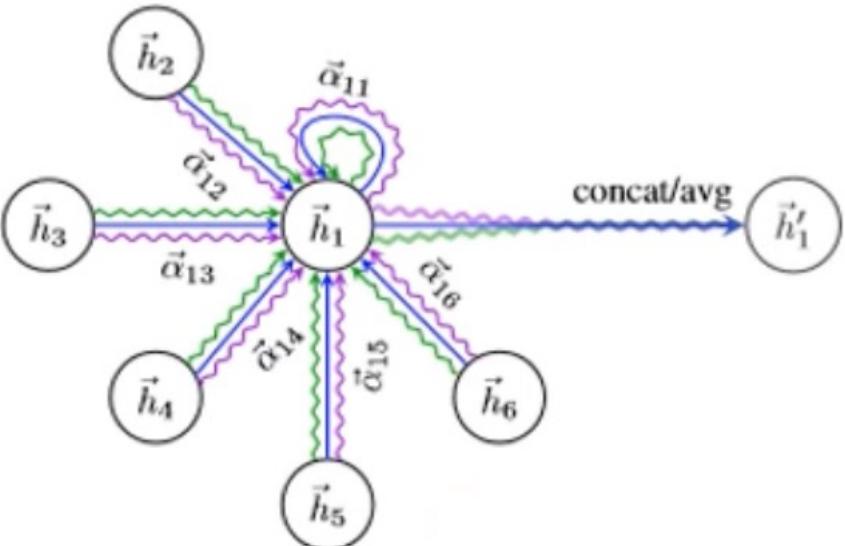
어텐션 스코어 a_{ij} 계산

Combine

이웃들의 정보 $a_{ij} Wh_j$ 합계

Multi-head attention

Readout



여러 개의 W를 사용
-> 여러 의미에서의 유사도
-> 여러 의미에서의 어텐션

여러 어텐션으로 계산된 값을
평균(concat)하여 성능 향상

4. Evaluation

Method	Cora	Citeseer	Pubmed
MLP	55.1%	46.5%	71.4%
ManiReg (Belkin et al., 2006)	59.5%	60.1%	70.7%
SemiEmb (Weston et al., 2012)	59.0%	59.6%	71.7%
LP (Zhu et al., 2003)	68.0%	45.3%	63.0%
DeepWalk (Perozzi et al., 2014)	67.2%	43.2%	65.3%
ICA (Lu & Getoor, 2003)	75.1%	69.1%	73.9%
Planetoid (Yang et al., 2016)	75.7%	64.7%	77.2%
Chebyshev (Defferrard et al., 2016)	81.2%	69.8%	74.4%
GCN (Kipf & Welling, 2017)	81.5%	70.3%	79.0%
MoNet (Monti et al., 2016)	81.7 ± 0.5%	—	78.8 ± 0.3%
GCN-64*	81.4 ± 0.5%	70.9 ± 0.5%	79.0 ± 0.3%
GAT (ours)	83.0 ± 0.7%	72.5 ± 0.7%	79.0 ± 0.3%

Node Classification Task (Transductive)

출처, 참고

<https://arxiv.org/abs/1710.10903>

<http://dmqm.korea.ac.kr/activity/seminar/296>